

## Communications: Power Analysis

### Earth-Lander Link

#### Carrier to Noise

- Rate 2/3 turbo code can achieve a C/N within 2 dB of Shannon Channel Capacity.
- C/N at Shannon Channel Capacity:

$$CNR = 2^{\frac{C}{B}} - 1 = 0.85175 \text{ dB} \quad (\text{at the Shannon Limit})$$

- C/N needed to achieve BER of  $10^{-6}$ : 2.85175 dB
- For our link budget calculations, we will add an addition C/N buffer and increase it to 4dB.

#### Path Loss

- Pathloss =  $20 \log_{10} \left( \frac{4\pi R}{\lambda} \right)$  dB
- R = 405,500 km (distance from earth to moon at apogee)
- Uplink Pathloss ( $\lambda = 0.04\text{m}$ ) = 222.103 dB
- Downlink Pathloss ( $\lambda = 0.0375\text{m}$ ) = 222.663 dB

#### Downlink Budget

- $P_T = \frac{C}{N} + P_N - G_R - G_T + \text{Pathloss}$
- $P_N = kT_{\text{sys}}B_N = 129.106 \times 10^{-15}$  (linear) = -128.433 dB
  - $T_{\text{sys}} = 44\text{K}$
  - $B_N = 5.625 \text{ MHz}$
  - $k = 1.38 \times 10^{-23}$
  - Multiply by 42 (number of elements in Allen Telescope Array)
- $G_R = h_A \left( \frac{pD}{\lambda} \right)^2 = 6.68543 \times 10^6$  (linear) = 68.2518 dBi (for all 42 elements)
  - $\lambda = 0.0375 \text{ m}$
  - $\eta = 0.63$
  - $D = 6\text{m}$
  - 42 Elements
- $G_T = 44.4 \text{ dBi}$
- C/N = 4 dB
- Pathloss = 222.663

- Link Budget Calculation:  $P_T = -14.4218 \text{ dBW} = 32.1263 \text{ mW}$

## **Uplink Budget**

- $P_T = \frac{C}{N} + P_N - G_R - G_T + \text{Pathloss}$
- $P_N = kT_{\text{sys}}B_N = 23.2875 \times 10^{-18} \text{ (linear)} = -166.329 \text{ dB}$ 
  - $T_{\text{sys}} = 50\text{K}$
  - $B_N = 33.75 \text{ kHz}$
  - $k = 1.38 \times 10^{-23}$
- $G_R = 37.4 \text{ dBi}$
- $G_T = 44.4 \text{ dBi}$
- $C/N = 4 \text{ dB}$
- $\text{Pathloss} = 222.103$
- Link Budget Calculation:  $P_T = -22.026 \text{ dBW} = 6.27 \text{ mW}$

## **Lander-Rover Link**

- In our link budget equations, we will assume a  $C/N$  of 20 dB to ensure near-errorless transmission
- Maximum gain of a half-wave dipole antenna is 2.15dB, so we will assume a worst-case gain of 1 dB for both transmit and receive antennas for the link budget.

## **Path Loss**

- To allow the rover to travel long distances from the lander but still communicate with it, we will assume a maximum communication distance of 10km.
- Uplink (Lander to Rover):
  - Carrier Frequency: 1 GHz
  - Pathloss = 112.442
- Downlink (Rover to Lander):
  - Carrier Frequency: 900 MHz
  - Pathloss = 111.527

## **Noise Power**

- Taking into account the device noise temperatures from the oscillators, mixers, amplifiers, and other RF devices in the link, we will assume a worst case  $T_{\text{sys}}$  of 400K.
  - Uplink (Lander to Rover):
    - $B_N = 22.5 \text{ kHz}$
    - $P_N = 124.2 \times 10^{-18} \text{ (linear)} = -159.059 \text{ dB}$
  - Downlink (Rover to Lander):
    - $B_N = 3.75 \text{ MHz}$

- $P_N = 20.7 \times 10^{-15}$  (linear) = -136.84dB

### ***Transmit Power***

- Uplink (Lander to Rover) = -28.617 dBW = 1.375 mW
- Downlink (Rover to Lander) = -7.313 dBW = 185.652 mW